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## 3 ANALYSIS OF AIR POLLUTION PARAMETERS USING 4 COVARIANCE FUNCTION THEORY

### 5 ANALIZA PARAMETRÓW ZANIECZYSZCZENIA POWIETRZA Z 6 WYKORZYSTANIEM TEORII FUNKCJI KOWARIANCJI

7  
8 **Abstract:** The paper analyses the intensity changes of three pollution parameter vectors in space and time. The RGB  
9 raster pollution data of the Lithuanian territory used for the research were prepared according to the digital images  
10 of the Sentinel-2 Earth satellites. The numerical vectors of environmental pollution parameters CH<sub>4</sub> (methane), NO<sub>2</sub>  
11 (nitrogen dioxide) and trace gas O<sub>2</sub> (oxygen dioxide) were used for the calculations. The covariance function theory  
12 was used to perform the analysis of intensity changes in digital vectors. Estimates of the covariance functions of the  
13 numerical vectors of pollution parameters or the auto-covariance functions of single vectors are calculated from  
14 random functions consisting of arrays of measurement parameters of environmental pollution parameters vectors.  
15 Correlation between pollution vectors depends on the density of pollution parameters and their structure. Estimates  
16 of covariance functions were calculated by changing the quantization interval on a time scale and using a compiled  
17 computer program using the Matlab procedure package. The probability dependence between the environmental  
18 pollution parameter vectors and trace gas of the territory in Lithuania and their change in time scale was determined.

19 **Keywords:** air pollution, methane, nitrogen dioxide, oxygen dioxide, correlation, covariance functions

## 20 Introduction

21 The effects of climate change are increasingly felt around the world: natural processes  
22 are changing, extreme meteorological and hydrological phenomena are increasing, rainfall  
23 patterns are changing, glaciers are melting, ocean levels are rising, and so on. Average global  
24 temperature is higher by 0.80 C when compared to pre-industrial levels. In order to avoid the  
25 adverse effects of irreversible climate change, global temperature must not rise more than 2.0  
26 C. However, no matter what adaptation and mitigation measures countries will take in the  
27 coming decades, the effects of climate change will continue to grow and worsen due to past  
28 changes and current greenhouse gas emissions. Therefore, it is necessary to monitor and  
29 predict. Emission of greenhouse gases, such as Carbon dioxide (CO<sub>2</sub>) and methane (CH<sub>4</sub>),  
30 also Nitrogen dioxide (NO<sub>2</sub>) and sulfur dioxide (SO<sub>2</sub>) into our environment receives the  
31 world's concern because it was considered responsible for the ever-increasing global  
32 temperature and the weather disasters [1-3]. That have a direct impact on the world's  
33 atmosphere. It is critical that effective identification and capture technologies be developed

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to reduce the amount of greenhouse gases into our environment. Global Monitoring for Environment and Security (GMES) is a joint initiative of the European Commission (EC) and the European Space Agency (ESA), designed to establish a European capacity for the provision and use of operational monitoring information for environment and security applications [4]. Based on global observations, GMES services, provided essential information in three Earth-system domains (atmosphere, marine and land) and three cross-cutting domains (emergency management, security and climate change). The Space Component, led by ESA, comprises five types of new satellites called Sentinels, which are being developed by ESA specifically to meet the observational requirements of GMES services [5]. The GMES dedicated missions include the development of a series of two spacecraft of the Sentinel-1, Sentinel-2 and Sentinel-3 missions. For the analysis of pollution parameters, we will use Sentinel-2 mission which provides continuity to services relying on SPOT and LANDSAT multispectral high-resolution optical observations over global terrestrial surfaces. Sentinel-2 provides 13 spectral bands from the visible (VIS) and the near infra-red (NIR) to the short wave infra-red (SWIR) at different spatial resolution at the ground ranging from 10 m to 60 m. The 4 bands at 10m has: the classical blue (490 nm), green (560 nm), red (665 nm) and NIR (842 nm). It is dedicated to land applications. The 6 bands at 20m: 4 narrow bands in the vegetation red edge spectral domain (705 nm, 740 nm, 775 nm and 865 nm) and 2 SWIR large bands (1610 nm and 2190 nm) dedicated to snow/ice/cloud detection, and to vegetation moisture stress assessment. The 3 bands at 60m dedicated to atmospheric correction (443 nm for aerosols and 940 for water vapour) and cirrus detection (1380 nm) [6]. Sentinel Data are available in the Copernicus Open Access Hub for free (<https://scihub.copernicus.eu/>). The geometric and radiometric image quality present in the article [4]. The literature recommends the following wavelengths ( $\lambda$ ) for gases detection [7-9] (Table 1).

Table 1

Spectral wavelengths of bands regions of study gases

Target Gas	$\lambda$ [nm]	Type of wavelengths	Spatial resolution of the Sentinel-2 data [m]
CH <sub>4</sub> CO <sub>2</sub>	1542- 1685	SWIR	20
NO <sub>2</sub>	760- 905	VNIR/SWIR	10
O <sub>2</sub>	765- 794	VNIR	20

Additionally, the authors of the article studying samples of data from the newest Copernicus mission dedicated to monitoring our atmosphere, it is the Copernicus Sentinel-5, which was launched from October 2017. It is the result of close collaboration between ESA, the EC, the Netherlands Space Office, industry, data users and scientists. The mission (Sentinel-5P) consists of one satellite carrying the Tropospheric Monitoring Instrument (TROPOMI) [10, 11]. There are three levels data products. In the geophysical data Level-2 are products types: CO<sub>2</sub>, NO<sub>2</sub>, CH<sub>4</sub> and others. Spatial resolution of data is 7×7 km. This data source is relevant for global gases situation analyses. The pixel size is too big and study area

71 – Lithuania territory do not have the gases information inside of Sentinel-5P data.  
72 Apparently, gas concentration areas are smaller than data pixel size. In the literature, the  
73 authors find a remote sensing approach where various sensors are integrated into an  
74 unmanned aerial vehicle (UAV) [12, 13]. The UAV systems are characterized by low cost  
75 and rapid detection of methane gas leakage.

76 Every year Lithuanian national GHG (Greenhouse Gas) emissions report provides  
77 information on direct ( $\text{CO}_2$ ,  $\text{CH}_4$ ,  $\text{N}_2\text{O}$ , HFC,  $\text{SF}_6$  and  $\text{NF}_3$ ) and indirect ( $\text{CO}$ ,  $\text{NO}_x$ , NMLOJ,  
78  $\text{SO}_2$ ) anthropogenic emissions by sources in Lithuania and absorption by absorbents  
79 (vegetation) [10]. The report gives the GHG as equivalent to  $\text{CO}_2$ , as various GHG are  
80 estimated based on their global warming potential (GWP). The GWP of  $\text{CO}_2$  equals 1,  $\text{CH}_4$   
81 - 25,  $\text{N}_2\text{O}$  - 298,  $\text{SF}_6$  - 22800,  $\text{NF}_3$  - 17200 and so on. 2015 Lithuania accounted for 0.47 %  
82 of EU-wide GHG emissions. Germany had the highest emissions of 20.93 % of the EU total.  
83 Germany, the United Kingdom, France and Italy together accounted for 53.34% of GHG  
84 emissions.

85 The authors propose to estimate gas quantities and concentrations by using auto-  
86 correlation and gas correlation (Image Cross-Correlation ICC) module based on RGB  
87 satellite image data of gas concentrations  $\text{CH}_4$ ,  $\text{NO}_2$ ,  $\text{O}_2$ , and  $\text{CO}_2$  (section 2.2). The  
88 correlation change of each pollution parameter on a time scale is determined depending on  
89 the change of time intervals, i.e. as the quantization interval changes. The magnitude of the  
90 correlation between pollutant parameters is affected by the digital image parameters pixel  
91 density and pixel brightness (intensity).

92 Aim of study work: Using the developed auto-correlation and cross-correlation  
93 algorithm, to determine the change and correlation of methane, nitrogen dioxide and oxygen  
94 concentration in the time scale in the images of pollution parameters obtained by the remote  
95 sensing method.

96

## 97 **Materials and Methods**

### 98 **Test area**

99 Test area were located in the Eastern of Europe; in Lithuania Covering Kaunas and  
100 Trakai districts ( $54^\circ 42' 57.6''\text{N}$   $24^\circ 57' 37.4''\text{E}$ ) (see Fig. 1).

101



102

103 a) b)  
104 Fig.1. Test area: a) Kariotiskes landfill location: 54° 42' 58" N, 24° 57' 33" E; b) Kazoliskes landfill  
105 location: 54°48'25.0"N24°49'15.0"E (Source: Google Earth)

106 In Vilnius region Lithuania have two large landfill sites (the largest landfills of unsorted  
107 municipal waste in Lithuania): Kariotiskes and Kazokiskes (Fig. 1). The Kazokiskes landfill  
108 currently operating in this region generates 230 tons of waste (2018). This landfill has been  
109 in operation since 1987 and was closed in 2008 because it did not meet modern environmental  
110 standards and was morally and technologically obsolete. More than 4 million cubic meters  
111 of unsorted rubbish have been accumulated. The closure work lasted 1.5 years. The garbage  
112 in the area of 30 ha is covered with special multi-layer constructions, a gas collection system  
113 is installed to prevent the release of toxic methane gas into the environment. In 2010, the first  
114 power plant in Lithuania to generate electricity from landfill gas was opened here. Similar  
115 projects are underway in other landfills in the region.

116 Kazokiskes landfill area is 27.1 ha (Fig. 1 (b)). It operated from the 2007 year. This  
117 landfill replaced the closed Kariotiskes landfill. Landfill safety is ensured by EU-compliant  
118 measures:

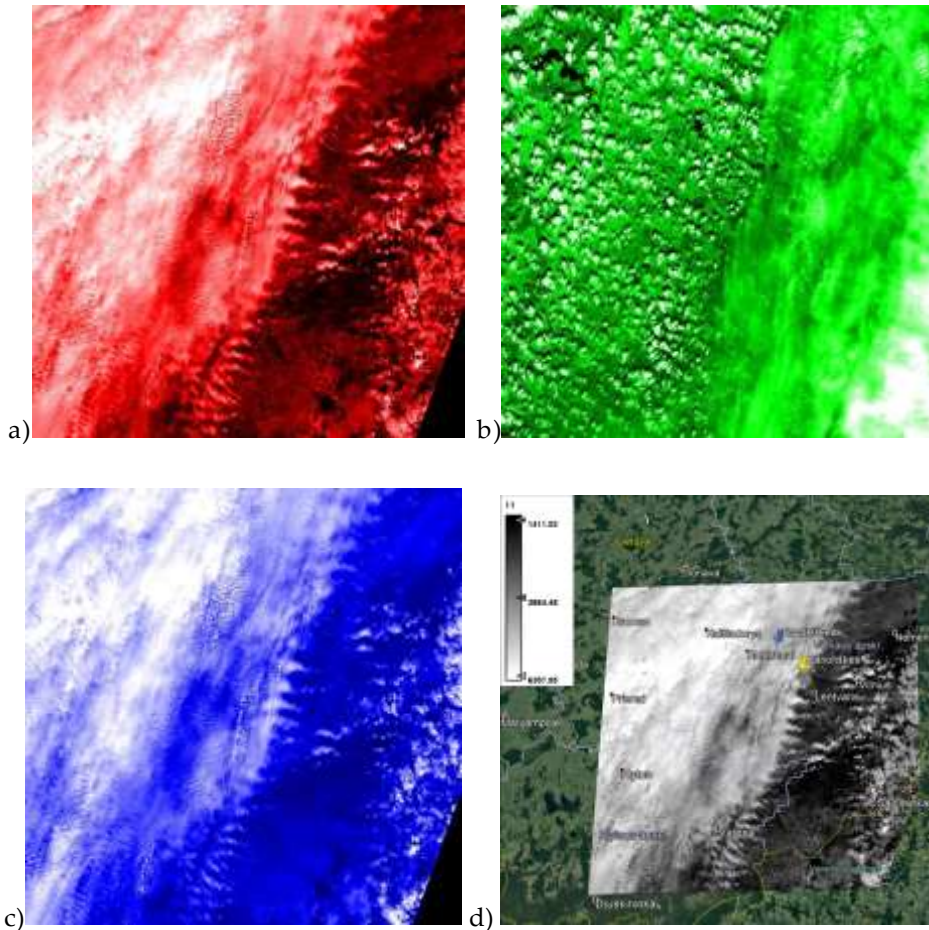
- 119 • A 0.5 m thick clay and high-density polyethylene geomembrane installed at the bottom  
120 of the landfill ensures that pollutants do not enter the environment;
- 121 • The filtrate formed in the landfill is collected in the drainage layer of granite gravel and  
122 enters the filtrate pumping station through pipes. The collected filtrate is sent for treatment  
123 to wastewater treatment plants;
- 124 • Groundwater monitoring wells were installed around the landfill: four in the direction  
125 of groundwater flow, one upstream. Gas monitoring is also carried out in wells, buildings  
126 and on the landfill.

127 Classical methods are used to monitor gas leaks in landfill areas, measured a couple of times  
128 a year with a multi-channel analyzer. The processes of gas accumulation and disintegration  
129 continue to take place in the closed landfill. It is important to monitor it continuously to avoid  
130 environmental consequences. Therefore, additional remote sensing studies have been made  
131 by authors in Kariotiskes landfill territory (Fig.1 (a)) [14].  
132

### 133 **Data acquisition**

134 Transformed digital image vectors of environmental pollution used for the study were  
135 prepared from satellite images. RGB-range CO<sub>2</sub>, NO<sub>2</sub> and CH<sub>4</sub> images data were obtained  
136 from Sentinel-2 mission MultiSpectral Instrument (MSI). Images needed were found through  
137 web interface of Copernicus Open Access Hub. This interface allows choosing territory and  
138 check availability of data filtered by date, product type and cloud cover for example. Products  
139 were chosen by Central wavelength (nm) and Bandwidth (nm) to correspond to wavelengths  
140 of possible CO<sub>2</sub>, NO<sub>2</sub> and CH<sub>4</sub> reflectance. The radiometric resolution of the MSI instrument  
141 is stored in 12-bit system, enabling the image to be acquired over a range of 0 to 4095  
142 potential light intensity values. The radiometric accuracy is less than 5% (goal 3%) [9, 10].  
143 Then using Sentinel-2 Toolbox software package satellite images processed to be rasterized  
144 and particular color applied in each case for grey-scaled intensity. In this study date of the  
145 images are 2019 May 12th and spatial resolution of bands are 10 meters and 20 meters  
146 covering roughly 109 x 109 km territory (see Fig. 2).

147



148 Fig.2. Raster images of spectral band intensities, which could possibly reflect pollution in Southeast part of  
 149 Lithuania: a) CH<sub>4</sub> ( $\lambda = 1542 - 1685$  nm); b) O<sub>2</sub> ( $\lambda = 765 - 794$  nm); c) NO<sub>2</sub> ( $\lambda = 760 - 905$  nm) d) CH<sub>4</sub>  
 150 greyscale overlay on satellite RGB images from Google Earth™

151 In the Fig. 2  $\lambda$  (Lambda) – Wavelength of spectral band. All three images cover the same  
 152 territory Southeast part of Lithuania. That area covers two parts of major districts of Lithuania  
 153 with various land uses. While the weather was partially cloudy, some matches between  
 154 spectral bands are visible. While each color is chosen artificially, instead of greyscale, it helps  
 155 to make computations simultaneously in RGB model.

156 **Methods: A covariance model of the intensity of environmental pollution parameter**  
 157 **vectors**

158 For the analysis of pollution parameters, the theory of covariance functions was used  
 159 [15-21]. Using this theory, it is possible to determine the strength of the dependence between  
 160 all the environmental pollution parameters considered. During the analysis, the variation of

161 normalized auto-covariance and inter-covariate functions of environmental pollution  
 162 parameter vectors  $\varphi$  with quantization interval was evaluated. The step of quantization  
 163 change is equal to the distance between the pixels in the image. The normalized auto-  
 164 covariance function values represent the variation of the correlation coefficients of the  
 165 individual pollution parameters over time, i.e. depending on the quantization intervals. The  
 166 normalized correlation function values represent the values of the correlation coefficients for  
 167 a single pollution parameter or two parameters (all pairs of parameters used) within the  
 168 respective quantization intervals.

169 Each column of a digital image pixel matrix is understood as a single pixel intensity  
 170 vector. The array of column-vectors of a matrix creates a transformed vector matrix  $B_i$  of  
 171 pixel intensity vectors of the transformed  $i$ -digital image. We obtain three matrices  $B_i$ , of  
 172 three pollution parameters: CH<sub>4</sub>, O<sub>2</sub> and NO<sub>2</sub> pixel intensity vectors, where  $i=1, 2, 3$ .  
 173 Column-vectors of each matrix form the parametric vector of the whole matrix.

174 Theoretical model of covariance functions is based on the concept of stationary random  
 175 function, considering that errors in field parameter measurements are random and possibly  
 176 systematic, i.e. the mean of their errors  $M\Delta = const \rightarrow 0$  their variance  $D\Delta = const$  and  
 177 the covariate function of the digital signals depends only on the difference in the arguments,  
 178 i.e. from the quantization interval on the time scale.

179 Estimates of the covariance function of two numerical parametric vectors of the  
 180 environmental pollution parameters or the auto-covariance function of a single parametric  
 181 vector are calculated by spreading digital data vectors in the form of random functions.  
 182 Discrete transformation is used to process digital signals [19, 22].

183 In the parametric vector  $\varphi$  of measurement data for each environmental pollution  
 184 parameter the trend of measurement data for that vector was eliminated. We will consider the  
 185 random function generated by the data of the vector of environmental pollution  $\varphi$  as  
 186 stationary (in the broad sense), i.e. its mean the covariate function depends only on the  
 187 difference  $\tau$  of the arguments. The auto-covariance function of one random vector or the  
 188 covariance function of two random vectors is written in [19-23]:  
 189

$$190 \quad K_{\varphi}(\tau) = M \left\{ \delta_{\varphi_1}(u) \times \delta_{\varphi_2}(u + \tau) \right\}, \quad (1)$$

191 or

$$192 \quad K_{\varphi}(\tau) = \frac{1}{T-\tau} \int_0^{T-\tau} \delta_{\varphi_1}(u) \times \delta_{\varphi_2}(u + \tau) \times du, \quad (2)$$

193 here  $\delta_{\varphi_1} = \varphi_1 - \underline{\varphi}_1$ ,  $\delta_{\varphi_2} = \varphi_2 - \underline{\varphi}_2$  – centered  $\varphi$  vectors, when eliminated trend  $\underline{\varphi}$ ;  $u$  – vector  
 194 parameter;  $\tau = k \times \Delta$  – variable quantization interval,  $k$  – number of units of measure,  $\Delta$  –  
 195 value of unit of measure;  $T$  – time;  $M$  – symbol of average.  
 196  
 197

198 Estimation of covariance function  $K'_{\varphi}(\tau)$  based on the available data on the measurement  
 199 of the pollution parameters shall be calculated as follows (Eq. 3):  
 200

$$201 \quad K'_{\varphi}(\tau) = K'_{\varphi}(k) = \frac{1}{n-k} \sum_{i=1}^{n-k} \delta\varphi_1(u_i) \delta\varphi_2(u_{i+k}), \quad (3)$$

202 here  $n$  – total number of discrete intervals (pixels).  
 203

204 Formula (3) can be applied in the form of an auto-covariate or a covariate function. When  
 205 a function is auto-covariant, vectors  $\varphi_1(u)$  and  $\varphi_2(u + \tau)$  are parts of single vectors, and when  
 206 they are covariate, they are two different vectors. The estimate of the normalized covariate  
 207 function is equal to:

$$R'_\varphi(k) = \frac{K'_\varphi(k)}{K'_\varphi(0)} = \frac{K'_\varphi(k)}{\sigma'^2_\varphi}, \tag{4}$$

208 here  $\sigma'_\varphi$  – estimate of the standard deviation of the random function.  
 209

210 The formula (5) used to eliminate the trend of the digital measurement data vector:  
 211

$$\delta_\varphi = \varphi - \underline{\varphi}, \tag{5}$$

212 here  $\delta_\varphi$  – data vector, with trend eliminated;  $\underline{\varphi}$  – vector trend.  
 213

214 Estimation of the covariance matrix of the  $I$  – vector of environmental pollution  
 215 parameters looks like this:  
 216

$$K'(\delta\varphi_i) = \frac{1}{n-1} \delta\varphi_i^T \delta\varphi_i, \tag{6}$$

217 The estimate of the covariance matrix of the two vectors  $i$  and  $j$  of the environmental  
 218 pollution parameters shall be written:  
 219

$$K'(\delta\varphi_i, \delta\varphi_j) = \frac{1}{n-1} \delta\varphi_i^T \delta\varphi_j, \tag{7}$$

220 here  $\delta\varphi_i, \delta\varphi_j$  – the dimensions of the vectors must be the same.  
 221

222 Estimates of covariance matrices  $K'(\delta\varphi_i)$  and  $K'(\delta\varphi_i, \delta\varphi_j)$  are reduced to estimates of  
 223 correlation coefficient  $R'(\delta\varphi_i)$  and  $R'(\delta\varphi_i, \delta\varphi_j)$ :  
 224

$$R'(\delta\varphi_i) = D_i^{-1/2} K'(\delta\varphi_i) D_i^{-1/2}, \tag{8}$$

$$R'(\delta\varphi_i, \delta\varphi_j) = D_{ij}^{-1/2} K'(\delta\varphi_i, \delta\varphi_j) D_{ij}^{-1/2}, \tag{9}$$

225 here  $D_i, D_{ij}$  – estimates of the corresponding covariance matrices  $K'(\delta\varphi_i)$  and  $K'(\delta\varphi_i, \delta\varphi_j)$   
 226 the diagonal matrices of the principal diagonal members.  
 227

228

238 The accuracy of the calculated correlation coefficients is defined by the standard  
 239 deviation  $\sigma_r$ , estimating its value according to the formula:

240

$$\sigma_r = \frac{1}{\sqrt{k}}(1 - r^2), \quad (10)$$

241

242

243 here  $k = 8000$ ;  $r$  – correlation coefficient. The highest estimate of the standard deviation is  
 244 obtained when  $r$  the value is close to zero in this case as well  $\sigma_r = 0.01$  when  $r \approx 0.5$  we

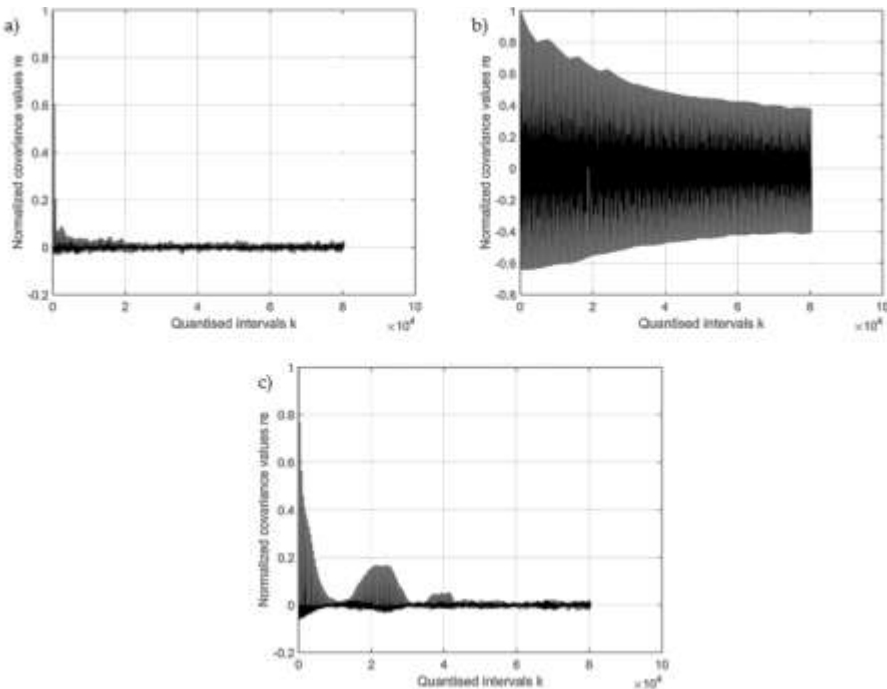
245 get  $\sigma_r = 0.08$ .

246

## 247 Experimental Results

248 Parameter vector measurement data was processed by compiled computer programs  
 249 using Matlab 7 software package operators. The  $k$  values of the quantization interval of  
 250 normalized covariate functions vary from 1 to  $n/2$  values, here  $n = 160000$  – number of  
 251 values of each parametric vector for environmental pollution. Normalized auto-covariance  
 252 functions were calculated for each parametric vector  $K_\varphi(\tau)$  estimate  $K'_\varphi(\tau)$  and graphical  
 253 expressions of 3 normalized auto-covariance functions were obtained. The quantization  
 254 interval is plotted on the abscissa axes and the values of the normalized covariate functions  
 255 (correlation coefficients) on the ordinates (see Fig. 3).

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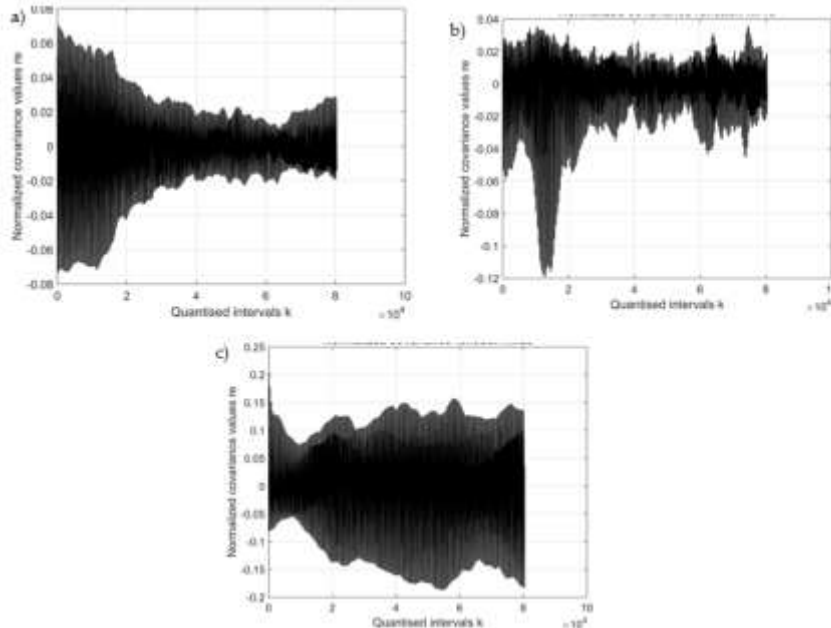
258 Fig. 3. Normalized auto-covariance function of pollution parameter of Lithuanian territory: a) of parameter  $CH_4$  ;  
 259 b) of parameter  $O_2$ ; c) of parameter  $NO_2$

260

261 Figure 3 (a) shows that as the quantization interval (pixel spacing) increases, the  
 262 correlation and particle density, which is simply proportional to the correlation, decreases to  
 263 zero  $r \rightarrow 1.0:0$  at about  $k = 40\ 000$ . The contamination  $O_2$  is greater than the contamination  
 264  $CH_4$ , because we have a higher correlation and hence a density ( $r \rightarrow 1.0:0.4$ ) (Figure 3 (b)).  
 265 Pollution  $NO_2$  is small, correlation coefficient  $r$  varies in the interval  $r \rightarrow 1.0:0.1$  to  $k = 50\ 000$   
 266 000 (Fig. 3 (c)). Correlation coefficient value is directly proportional to the density of  
 267 pollution.

268 In summary, the normalized auto-covariance functions take the highest value of the  
 269 correlation coefficient  $r \rightarrow 1.0$  at the values of the quantization interval  $k \rightarrow 0$  and continue  
 270 to decrease in the corresponding vectors to  $r \rightarrow 0$ . As the quantization interval increases, the  
 271 values of the auto-covariance functions decay to  $r \rightarrow 0$  at  $k \rightarrow 80\ 000$ ,  
 272 indicating a decrease in pollution with time. indicating a decrease in pollution with time.

273 To compute the normalized covariance functions  $K'_\varphi(\tau)$  estimates for all 3 parametric  
 274 vectors and 3 graphical expressions were obtained (see Fig. 4).



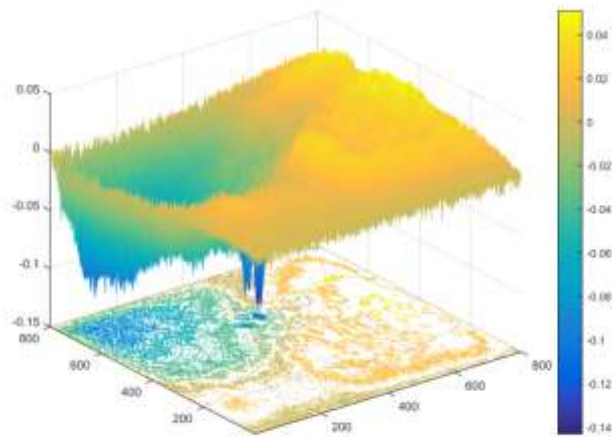
275

276 Fig.4. The normalized covariance function of the parametric vectors of pollution of the territory in Lithuania: a)  
 277 parameters  $CH_4$  and  $O_2$  ; b) parameters  $CH_4$  and  $NO_2$  ; c)  $O_2$  and  $NO_2$

278

279 There is little covariance between all the parameters of environmental pollution. Graphic  
 280 expressions for dependency change are different (see Fig. 4). The correlation between  
 281 pollution parameters  $CH_4$  and  $O_2$  is small, changing in the interval  $r \rightarrow -0.07: +0.07$  (see  
 282 Fig. 4 (a)). The correlation between pollution parameters  $CH_4$  and  $NO_2$  is practically close  
 283 to zero. Small bumps were observed, possibly due to random variation of density (see Figure  
 284 4 (b)). The correlation between pollution parameters  $O_2$  and  $NO_2$  is small, the values of  
 285 correlation coefficient vary in the interval  $r \rightarrow -0.18: +0.2$  (see Fig. 4 (c)).

286 A graphical representation of the generalized (spatial) correlation matrix is shown in Fig.  
 287 5.



288 Fig.5. Graphical representation of a generalized (spatial) correlation matrix of 3 parameters of the Kariotiskes  
 289 landfill environment pollution:  $CH_4$ ,  $O_2$ , and  $NO_2$  parametric vectors  
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The expression of the correlation matrix takes the form of a block of 3 pyramids, in which the values of the correlation coefficients are represented by the shades of the color spectrum (Fig. 5). Value of correlation coefficient vary from  $-0.15$  (blue color) to  $0.05$  (yellow color). The blue color shows that the normalized auto-covariance contamination  $O_2$  is greater than  $CH_4$  and  $NO_2$  like on the results of Fig. 3.

## 298 Conclusions

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Detecting in time and monitoring gas emissions from an area quickly and accurately is not an easy task. Payloads that are based on the integration of easy to operate and cost-effective methane or other gases detectors are preferred for routine monitoring compared to expensive and complex ones. One way to improve the monitoring is by enhancing the quality and the quantity of the collected data [12]. Integrating information from free data - satellite images can improve the measurement process and accelerate identification methods. The study showed that the result is influenced by the spatial resolution of the photos, on which depends the pixel size, density and pixel brightness (intensity). The concentration of gas in the atmosphere can be estimated from the available 12 bit information on the intensity of pixels in RGB photo and their auto-correlation and correlation.

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The study found that the expressions of the normalized auto-covariance functions of all three pollution parameters:  $CH_4$ ,  $O_2$  and  $NO_2$  are different, while the pollution parameter  $O_2$  has values throughout the quantization range. This indicates that the density structures of the above mentioned pollution parameters are also different.

There is little mutual covariance between the pollution parameters:  $CH_4$ ,  $O_2$ ,  $NO_2$ , and  $CO_2$ , because the values of the normalized covariance functions of their parametric functions are close to zero. Thus, the correlation between environmental pollution parameters is rather

316 weak and possibly due to the low density of pollution parameters and their structures are  
317 sufficiently different.

### 318 **Conflict of Interest**

319 The author declares that there is no conflict of interests regarding the publication of this  
320 paper.

### 321 **Acknowledgment**

322 This research was performed as part of the employment of the authors at Vilnius  
323 Gediminas Technical University as employees and PhD student.

### 324 **Data Availability statement**

325 The digital images of the Sentinel-2 data used to support the findings of this study have  
326 been deposited in the Open Science Framework repository (<https://osf.io/s98uz/>).

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